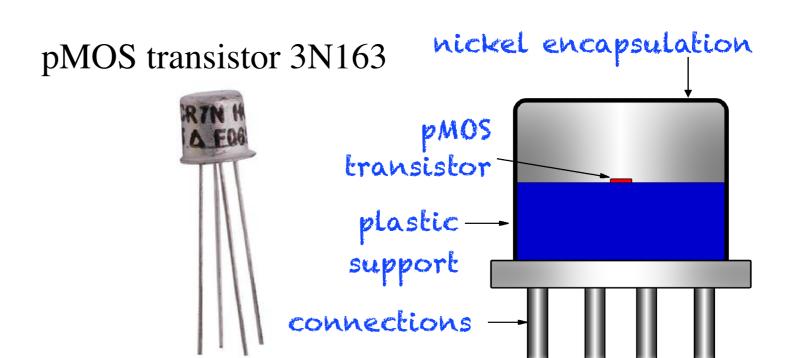
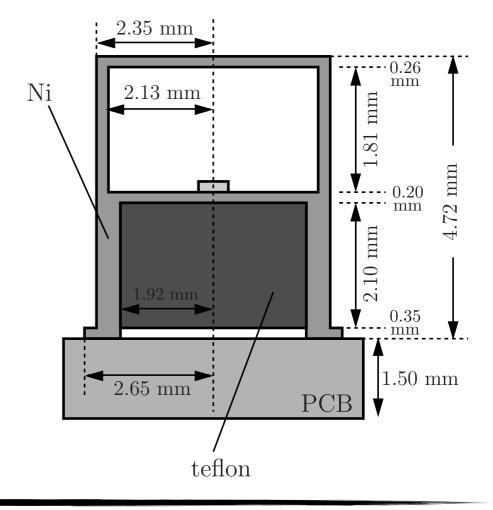


#### pMOS transistor 3N163

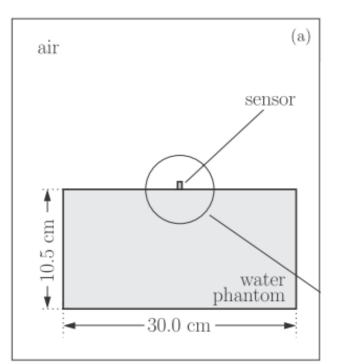


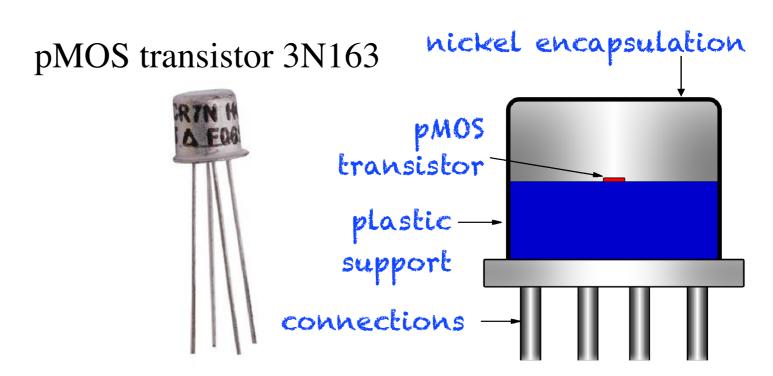


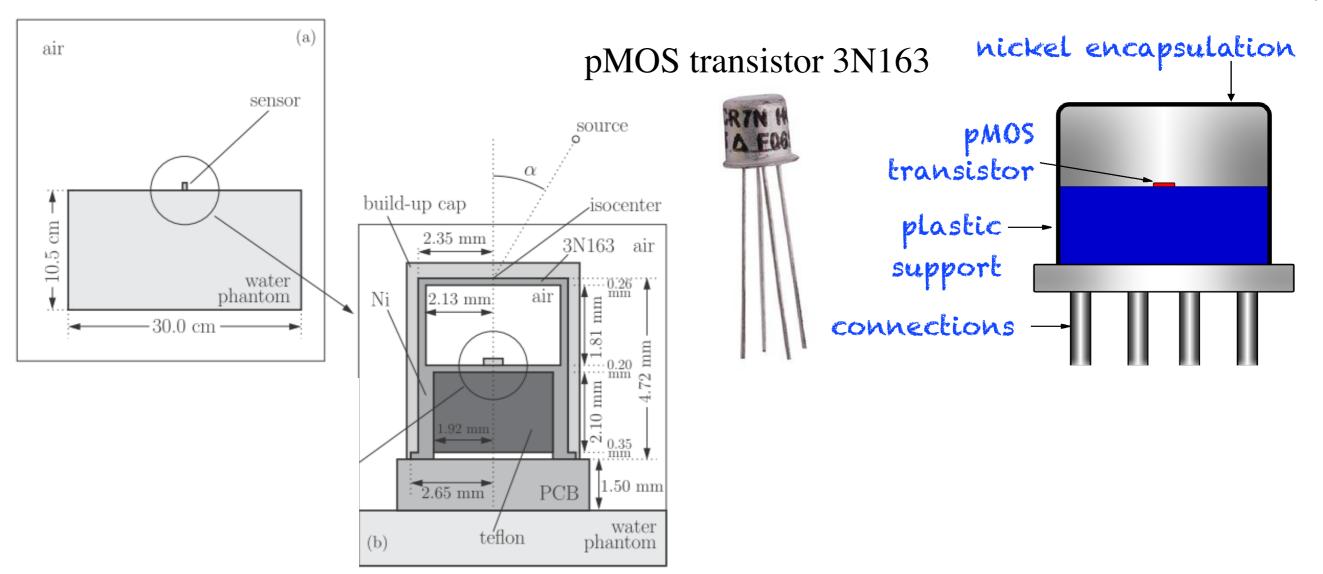


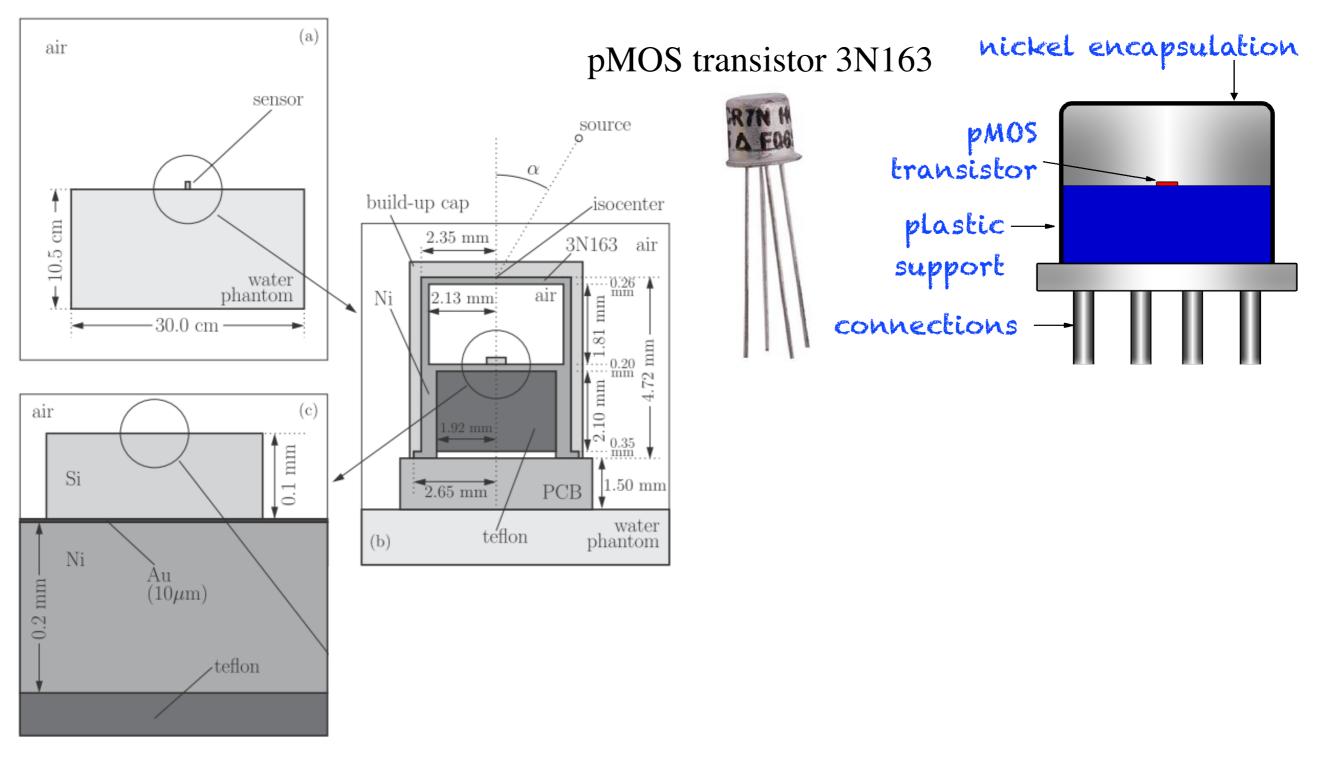
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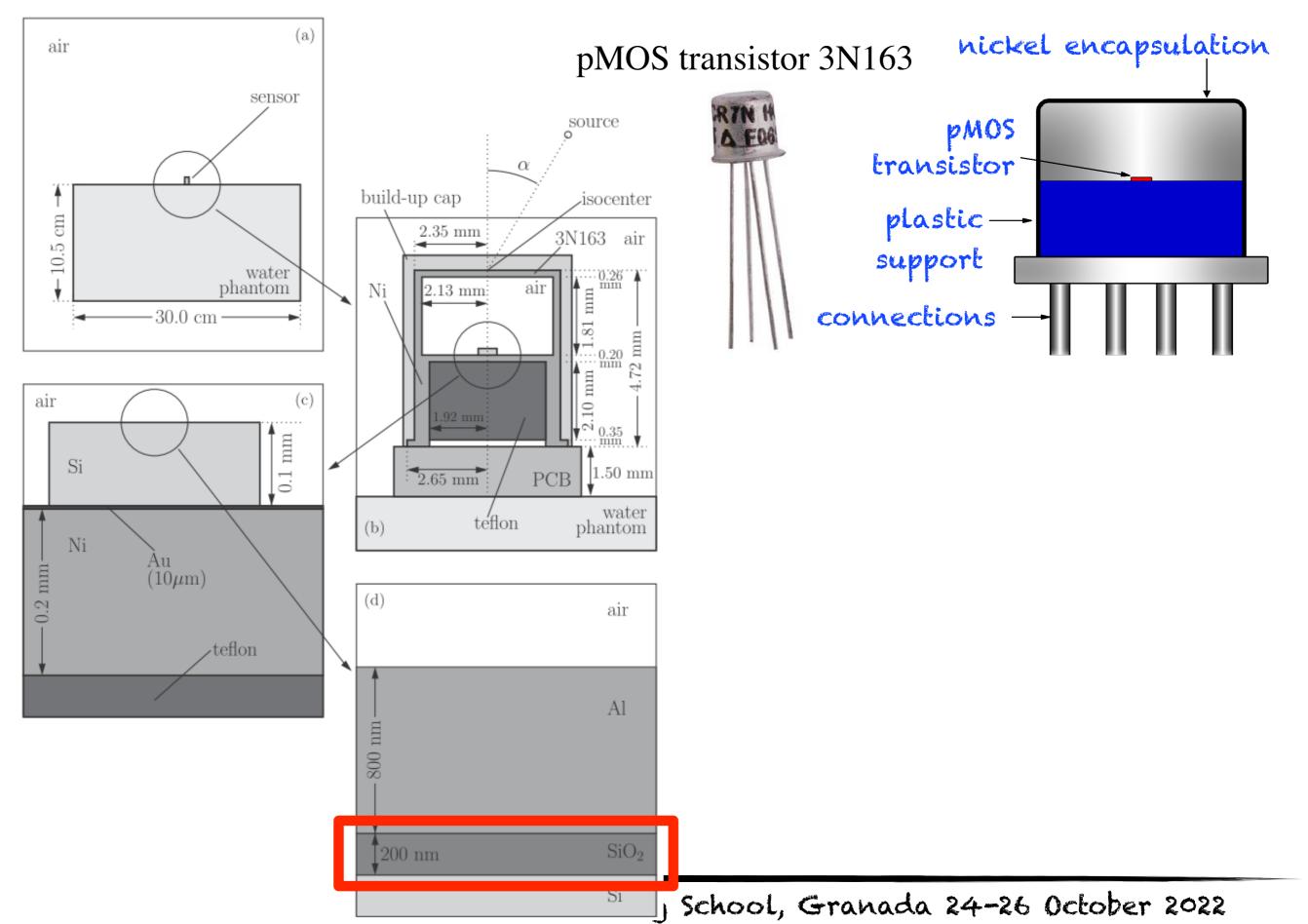
pMOS transistor
plastic
support
connections

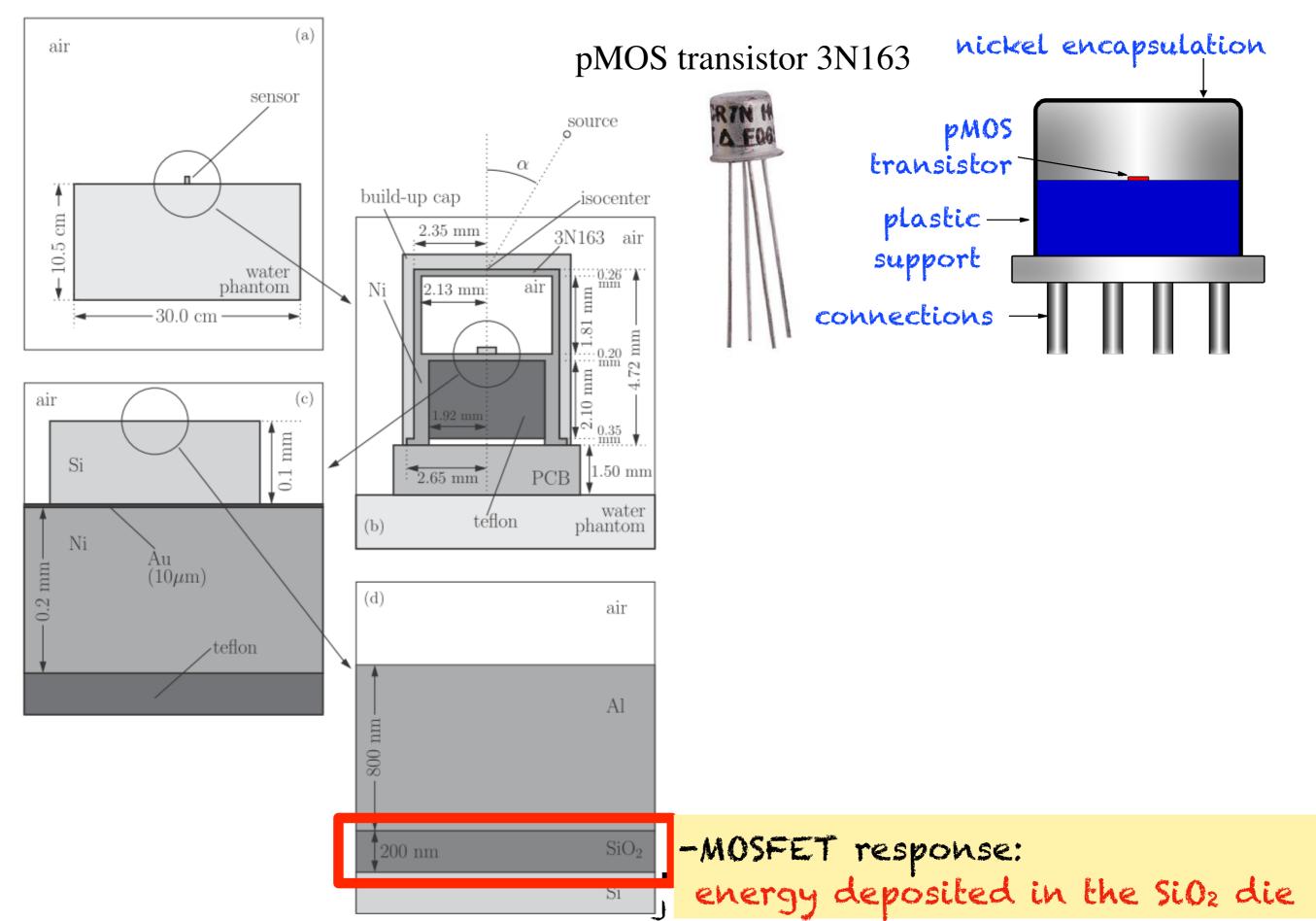


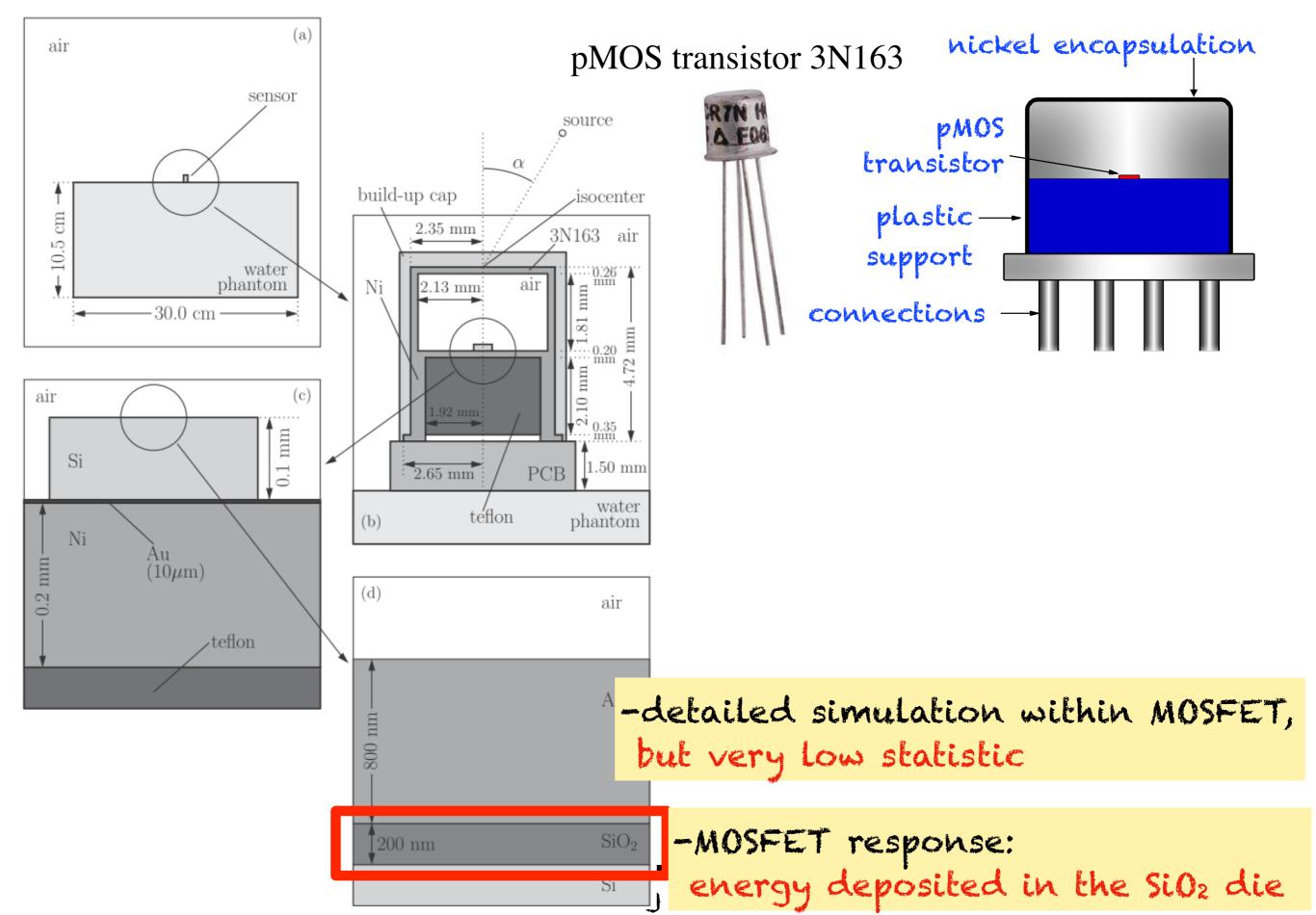


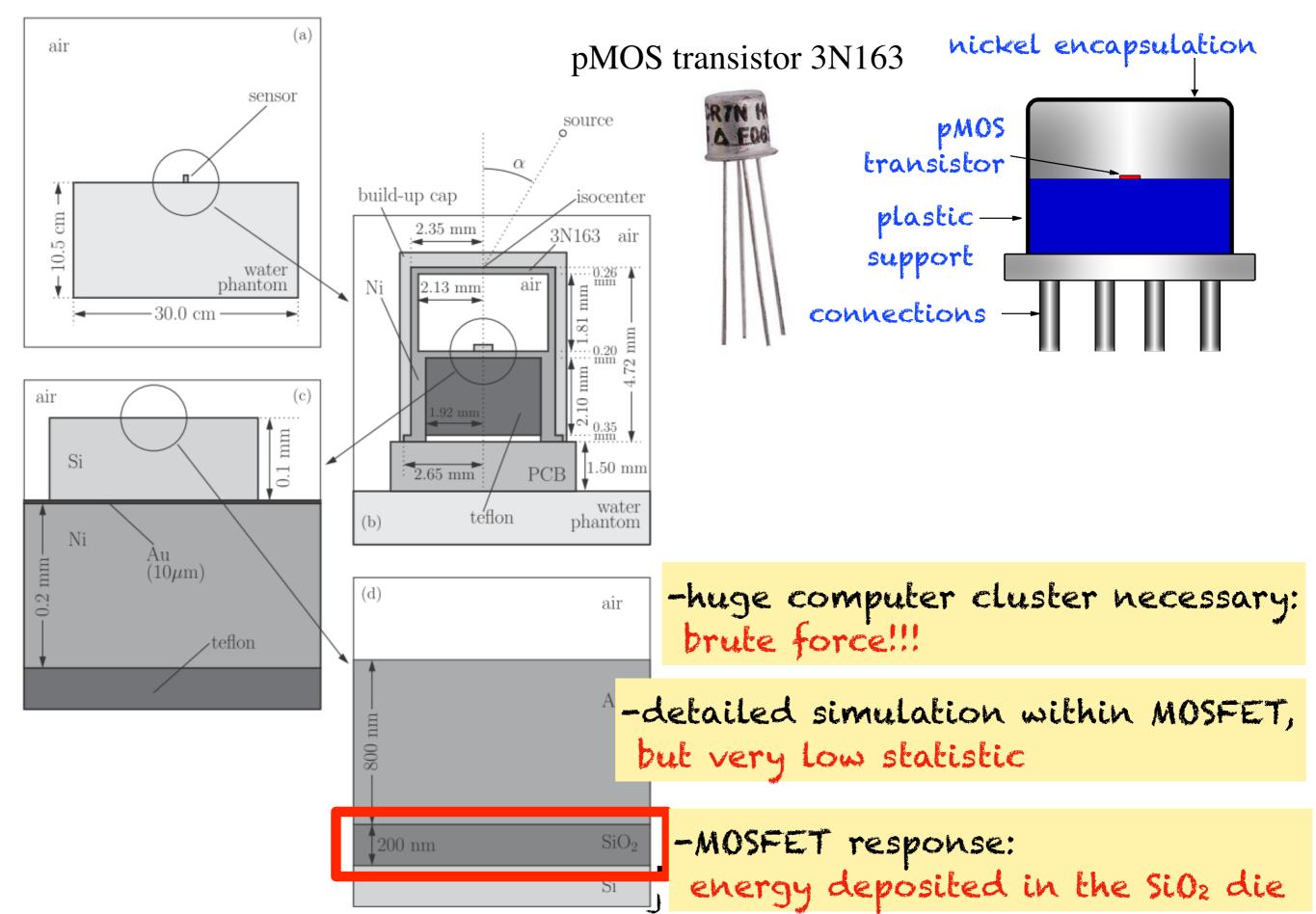


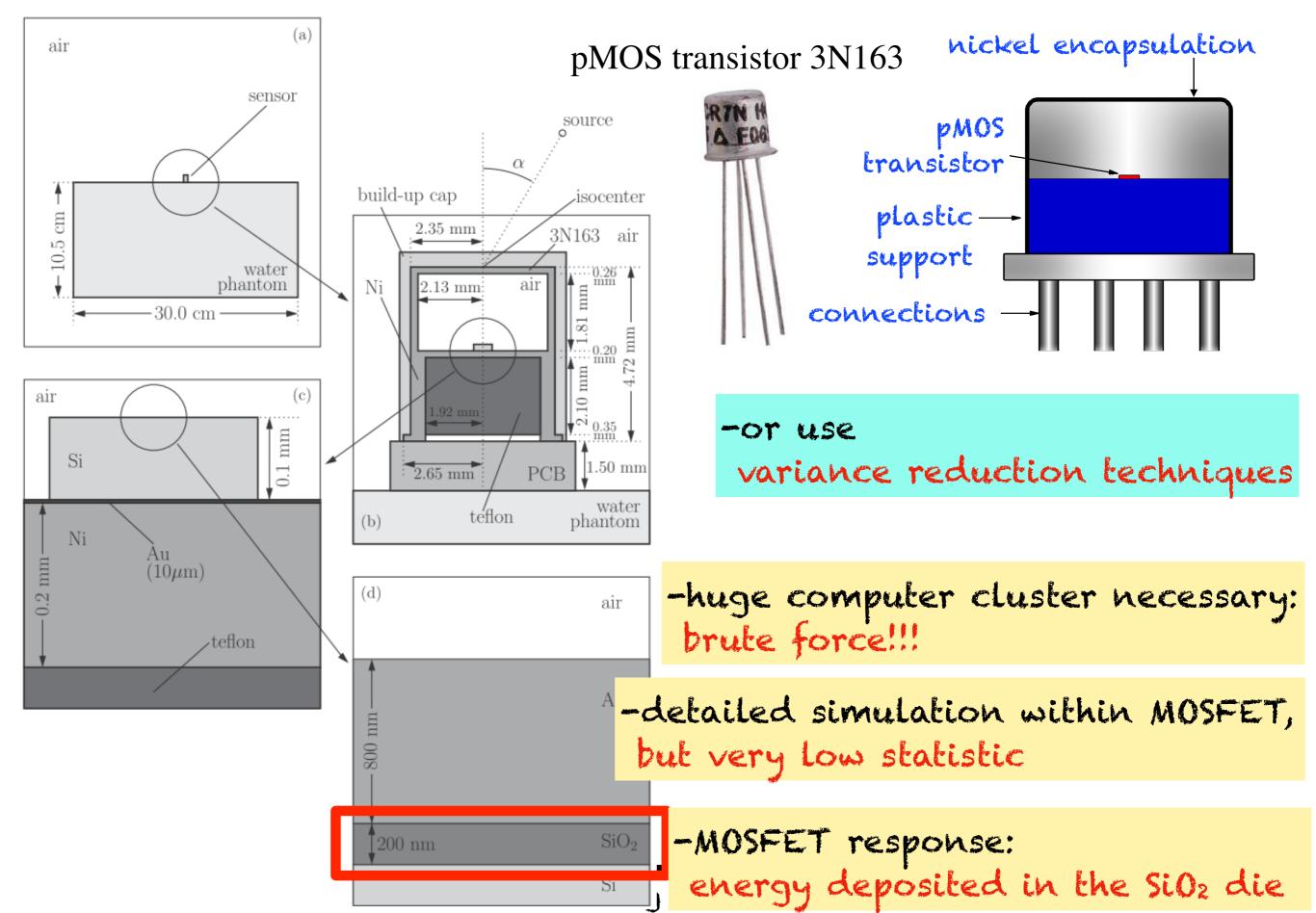














# Variance reduction techniques in Monte Carlo simulations: ants at work!

Salvador García-Pareja

Hospital Regional Universitario, Málaga, Spain



Universidad de Granada, Spain



UNIVERSIDAD DE GRANADA



# Outline

- Introduction
- ·Ant colony algorithm
- · Results
- Conclusions



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how to do it?





Russian roulette

•Russian roulette

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a particle in a state  $(\mathbf{r}, E, \hat{\mathbf{d}})$ , with weight  $w_0$ , moving towards a RoI, is transformed in  $\mathcal{S} > 1$  particles, in the same state, with weight  $w = w_0/\mathcal{S}$ 



#### Russian roulette

a particle with weight  $w_0$ , moving away from the RoI, is "killed" with probability  $\mathcal{K}$   $(0 < \mathcal{K} < 1)$ ; if it survives, its weight becomes  $w = w_0/(1 - \mathcal{K})$ 

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VRT effectiveness depends on:

- $\bullet$   $\mathcal{S}$  and  $\mathcal{K}$  values
- strategy used for splitting and killing



- -ants look for food following random walks
- -if food is found, ants come back to the nest
- depositing pheromone
- -ants tend to follow paths with the largest
- level of pheromone
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- -a particle source and a RoI are defined -the whole geometry is divided into virtual cells -each cell is characterized by an importance value

$$P_i = \frac{W_i^{\text{C}}}{W_i^{\text{P}}}$$
 sum of the weights of particles entering *i*-th cell and that reach the RoI (they or their descendants) sum of the weights of particles entering *i*-th cell

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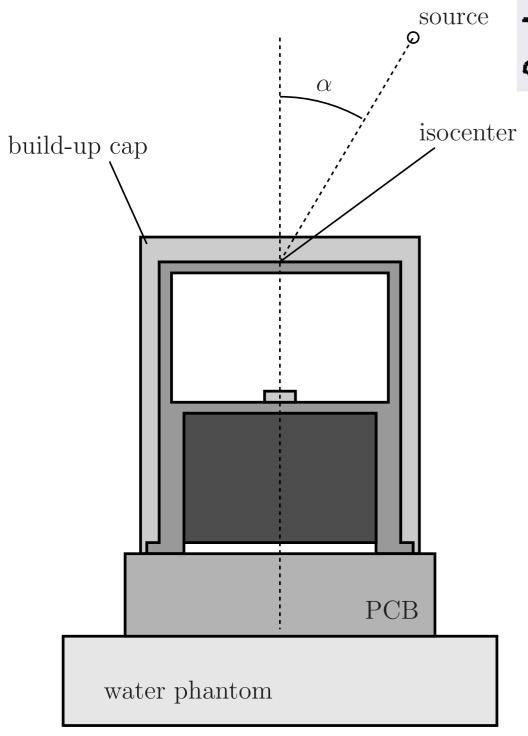
eif w·I=1: do nothing

Results

Results

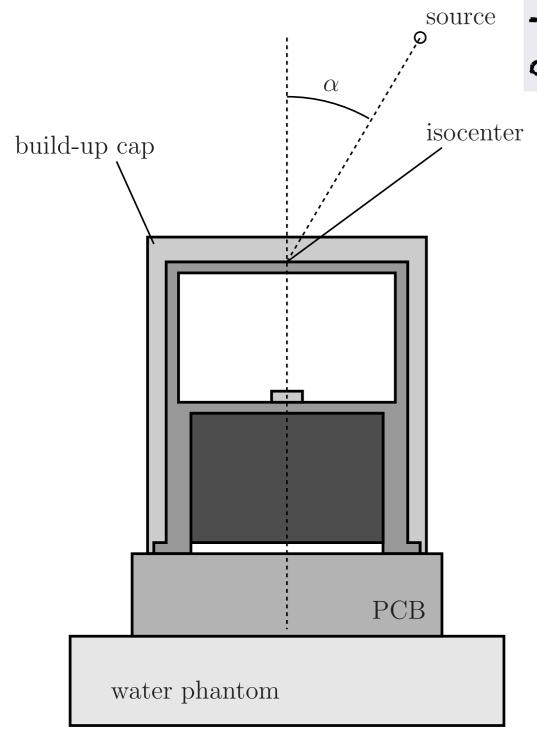
# MOSFET used as a in-vivo dosimeter

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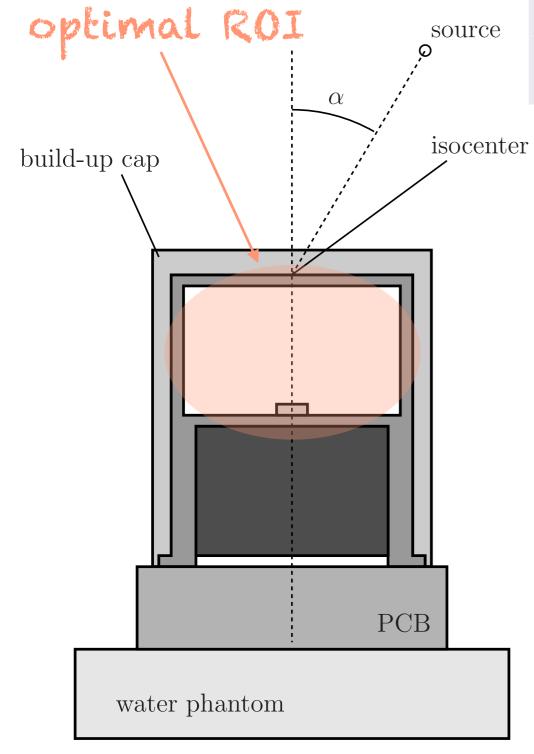
-the algorithm does not work!!

-because of the few number of particles reaching the RoI,

•filling the importance map to begin applying VRT takes a large CPU time (1000 particles reaching the RoI)

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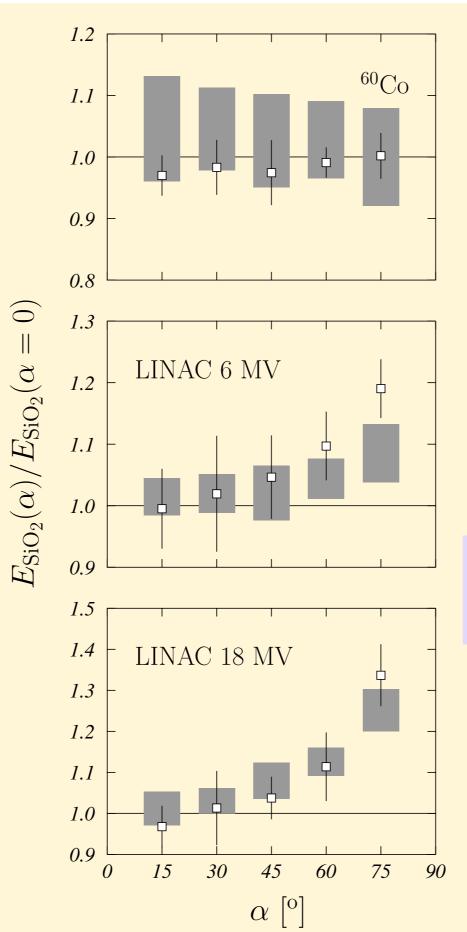
  •filling the importance map to begin applying VRT takes a large CPU time (1000 particles reaching the RoI)

  •actualization of the importance map is extremely slow and uncertainties remain huge
- optimal RoI:

   -whole Si die + SiO<sub>2</sub> + air
   -a gain factor ~70 to fill the importance map and "human" CPU times to reach reasonable uncertainties

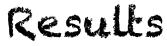
Results

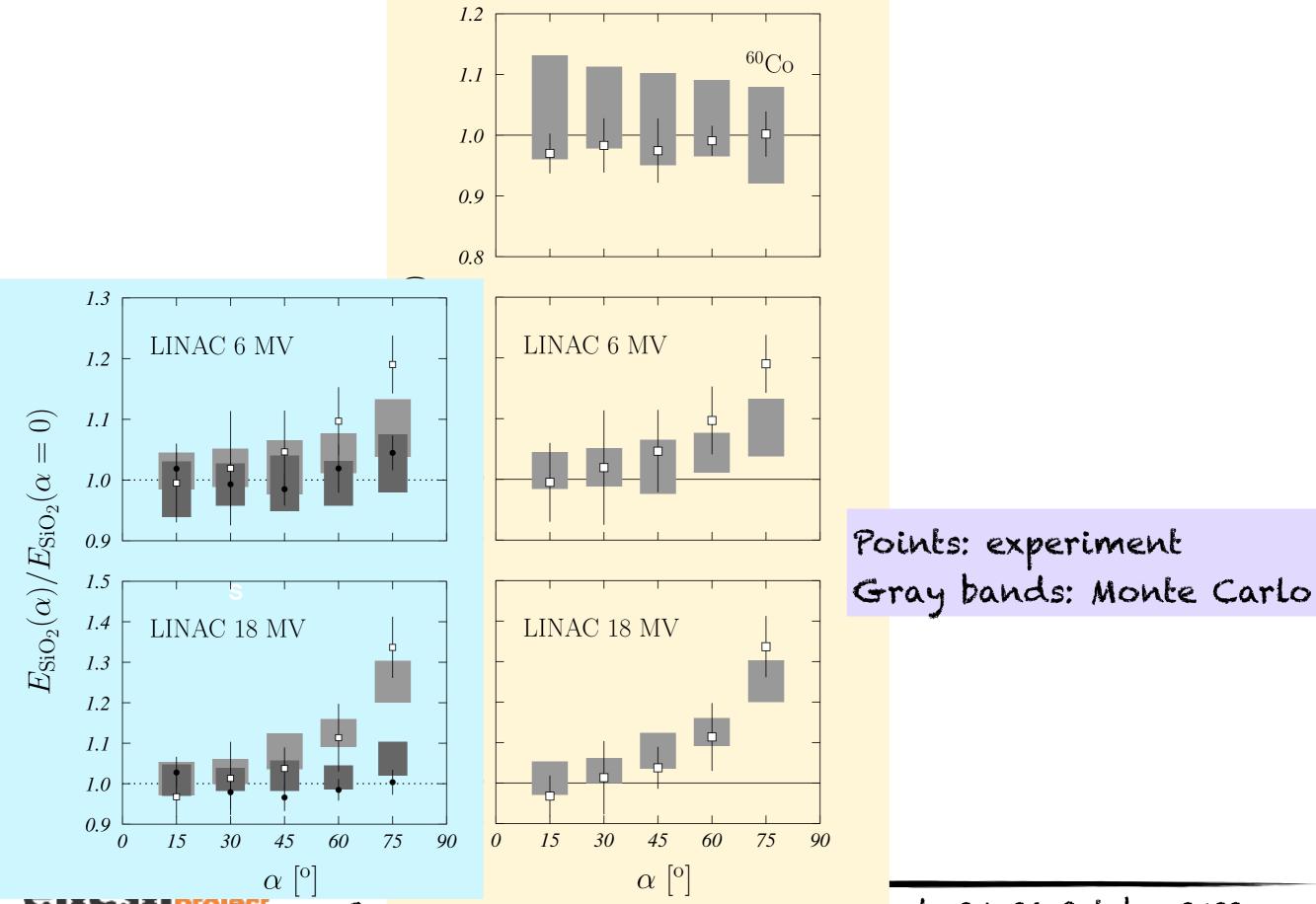
### Results



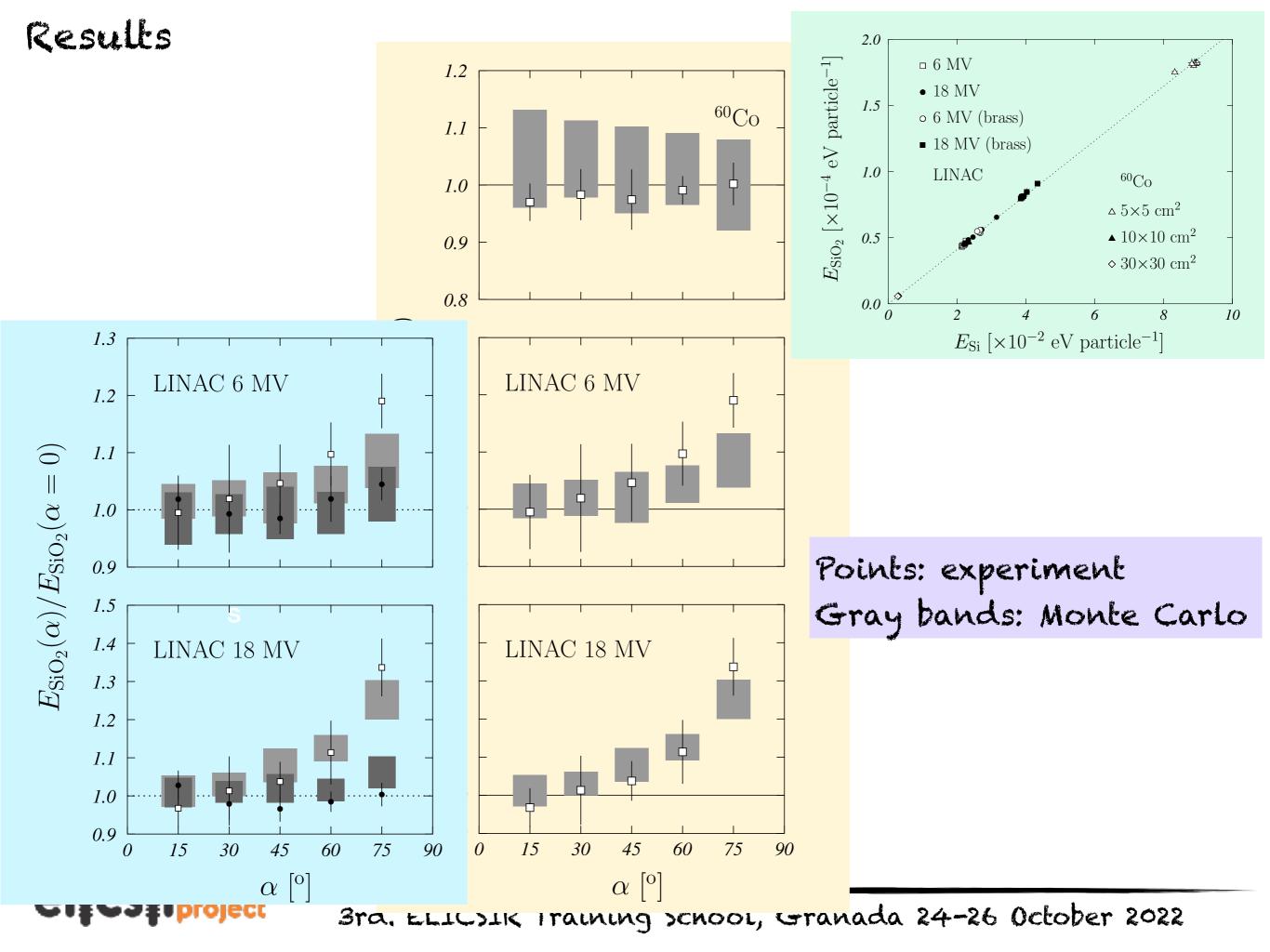
Points: experiment Gray bands: Monte Carlo







3ra. ELICIK Iraining school, Granada 24-26 October 2022



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- The ant colony algorithm developed allows the efficient implementation of VRTs by using the information scored on importance maps and with a minimum intervention of the user ... but details are relevant
- ·Applications in other problems:
  - -clinical linacs
  - -radiosurgery photon beams (very small fields)
  - -specific absorbed fractions (nuclear medicine)
  - -correction factors of small ionization chambers



- M. Anguiano Univ. Granada (Spain)
- G. Díaz Londoño Inst. Tech. Metropolitan Medellín (Colombia)
- F. Salvat Univ. Barcelona (Spain)
- L. Brualla Universitatsklinikum Essen (Germany)
- A. Palma, M.Á. Carvajal Univ. Granada (Spain)
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- F. Erazo SOLCA Cuenca (Ecuador)
- M. Vilches IMOMA Oviedo (Spain)
- P. Galán Hosp. Univ. Málaga (Spain)

# Variance reduction techniques in Monte Carlo simulations: ants at work! S. García-Pareja, A. M. Lallena



Thanks !!







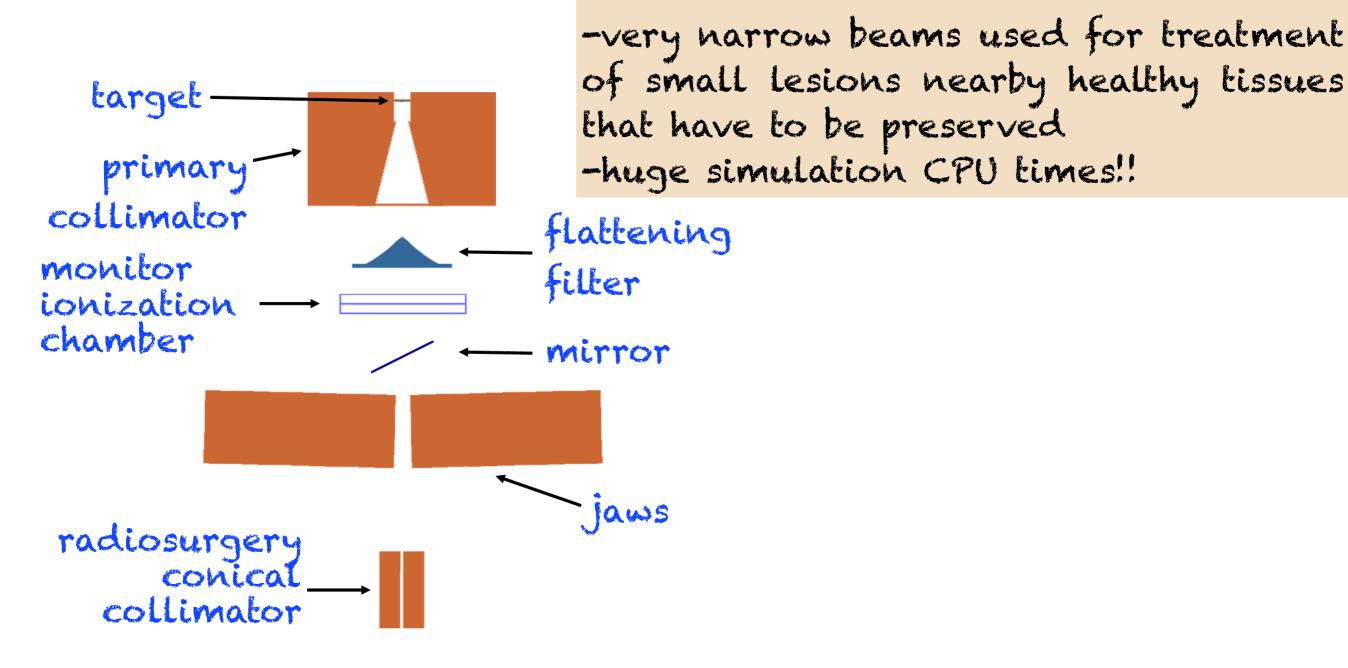
### Photon beams for radio surgery

-very narrow beams used for treatment of small lesions nearby healthy tissues that have to be preserved -huge simulation CPU times!!





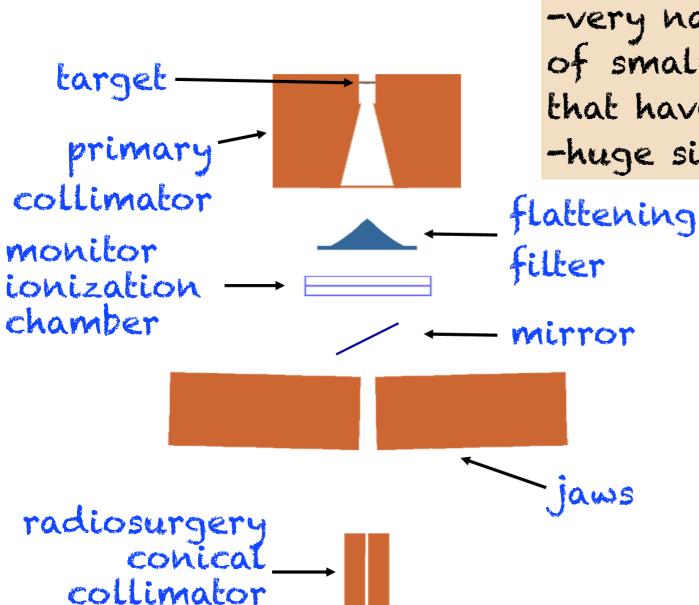








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-VRT applied to both electrons and photons

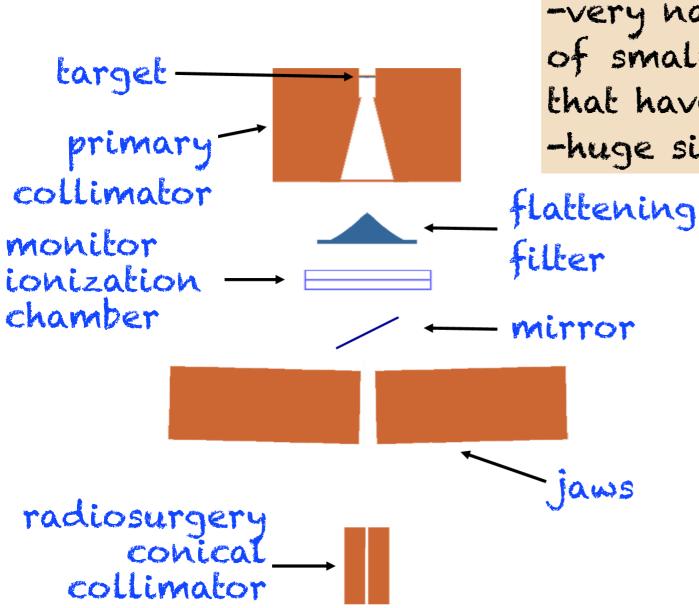
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directional Bremsstrahlung splitting is needed
 applied throughout the whole geometry



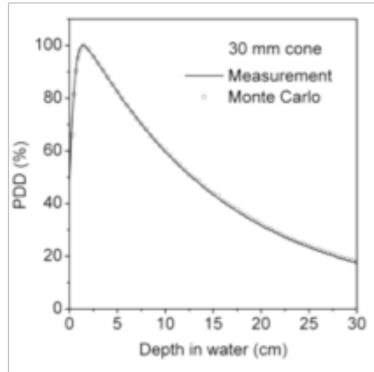


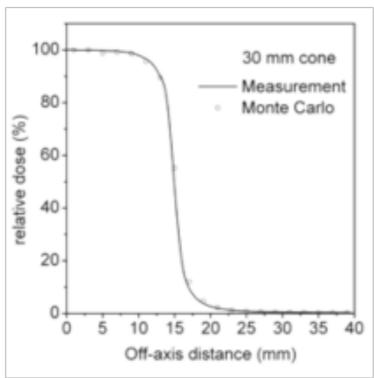










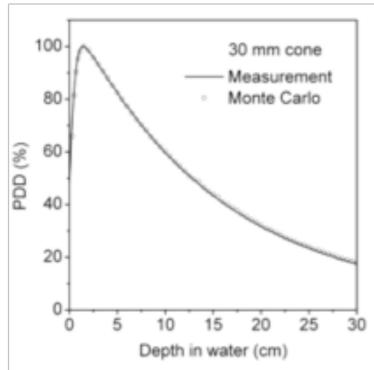


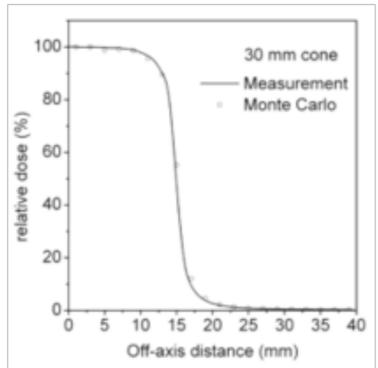






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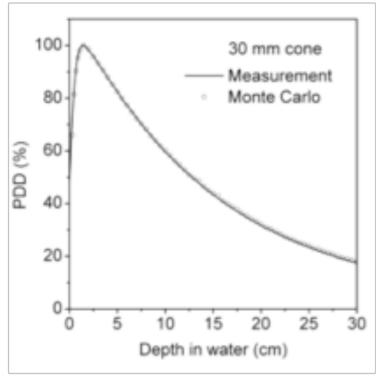
CPU times: 9 h (10 mm) to 0.9 h (30 mm)

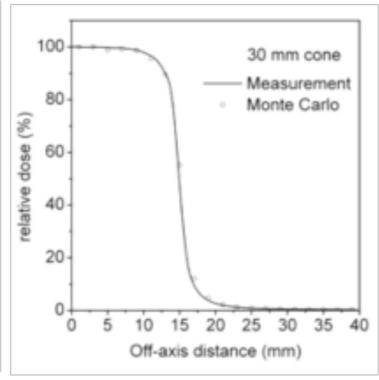






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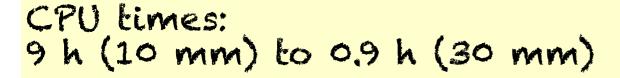


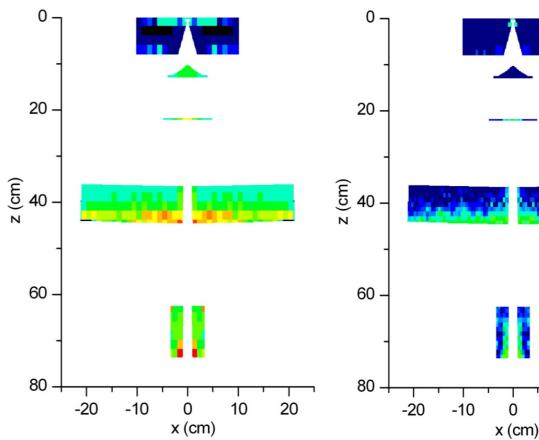


high energy electrons

20

10











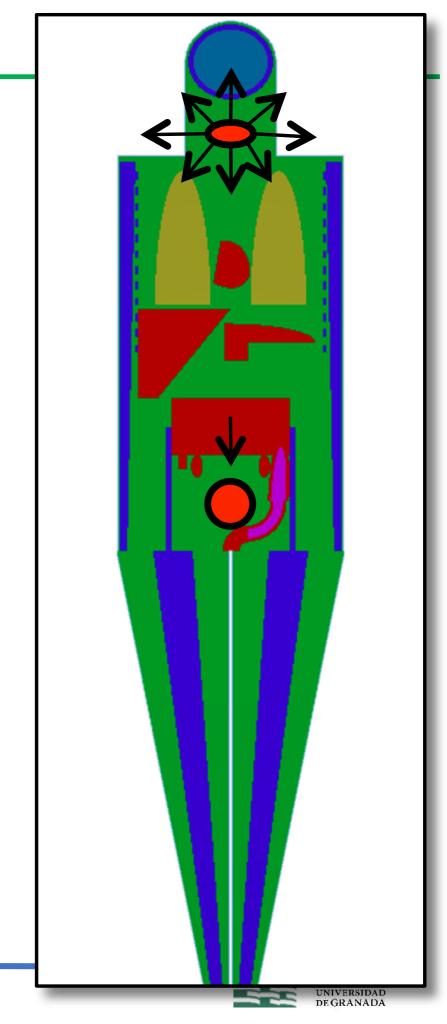








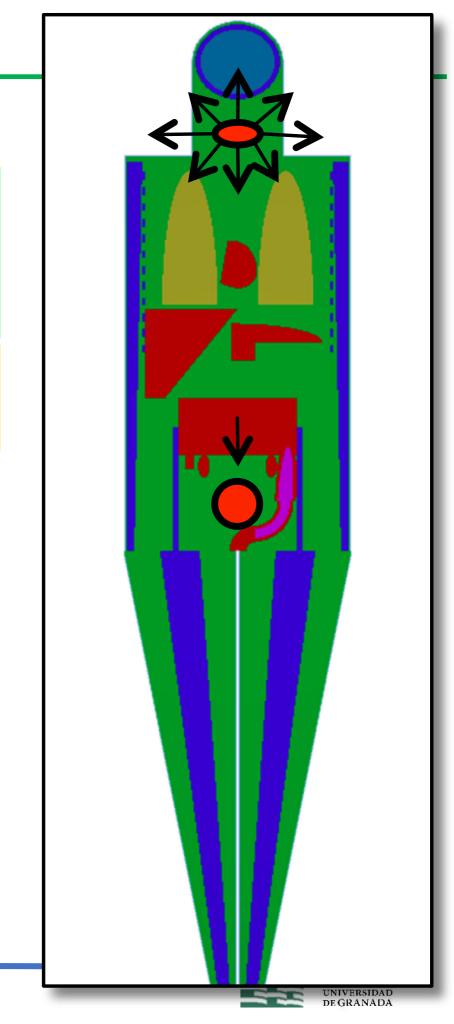
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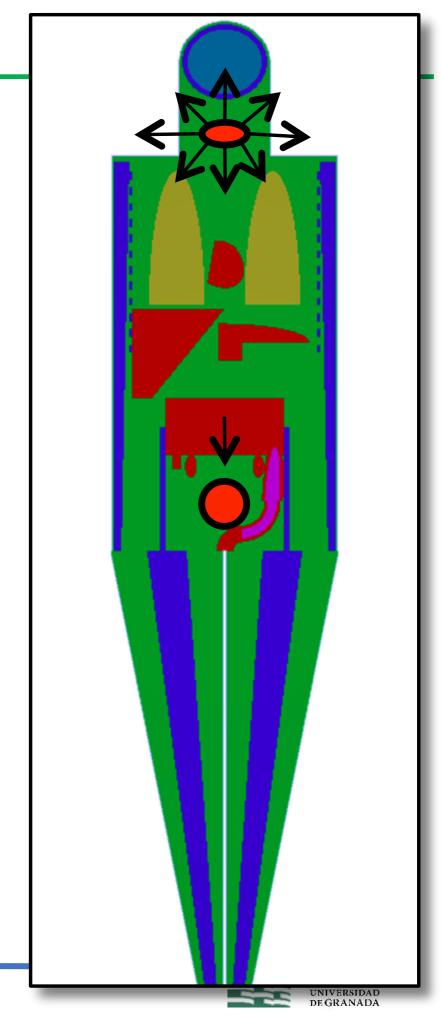




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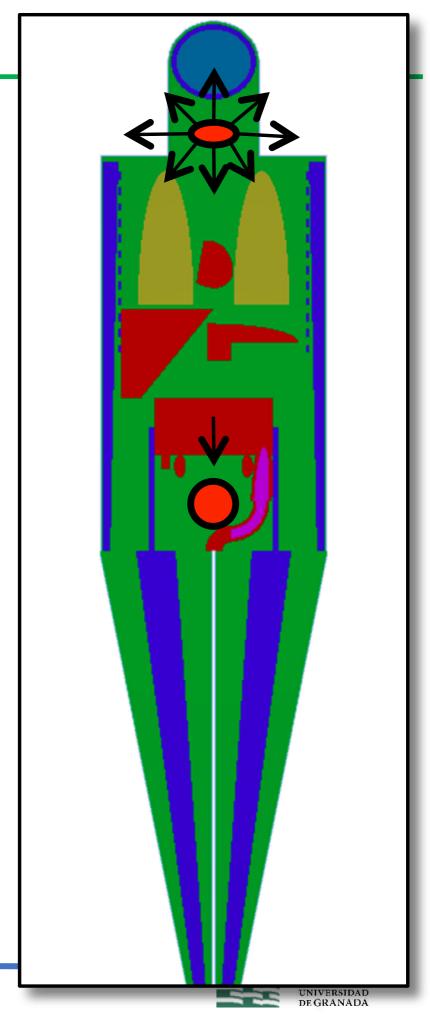


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## Correction factors of micro-chambers





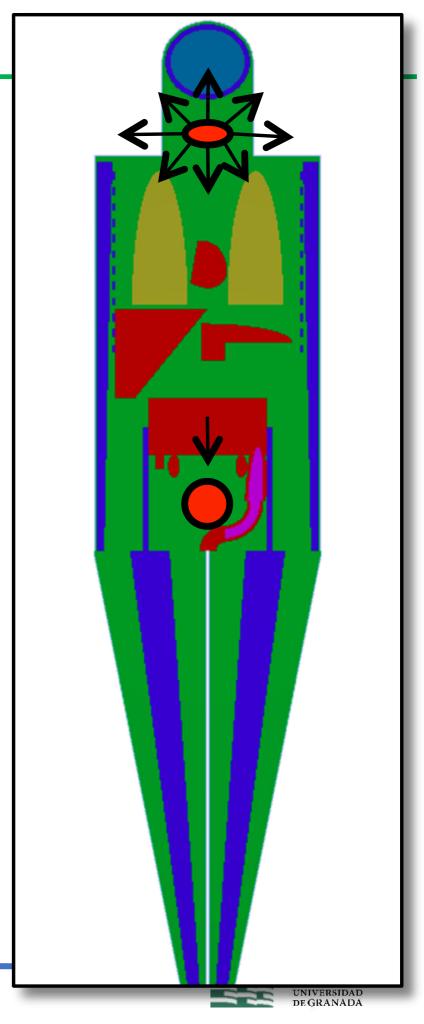
-inform about organ/tissue irradiation due to diagnostic or therapy of other organ
-interest in Nuclear Medicine

-problem: very low statistics because of organ volume and/or distance to source

-efficiency increase by a factor 10!!

reproject

Correction factors of micro-chambers



## Some applications Specific absorbed

### Specific absorbed fractions

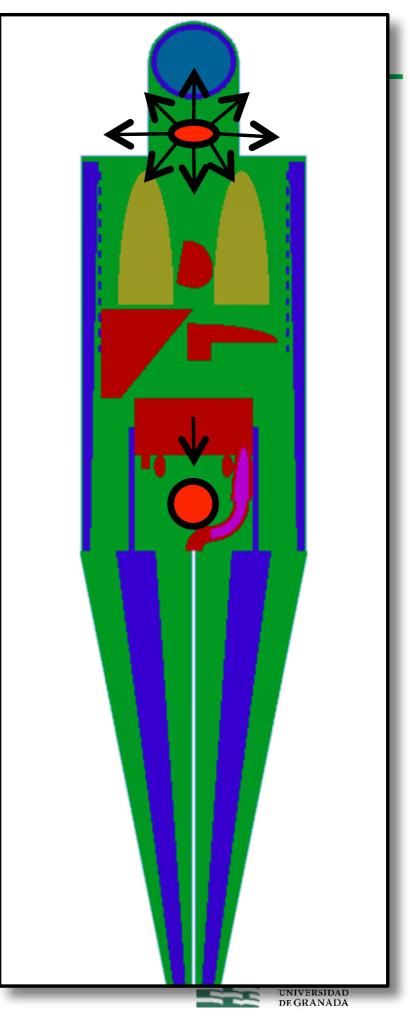
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-efficiency increase by a factor 10!!

Correction factors of micro-chambers

-efficiency increases by a factor 100!!





roject

#### Conclusions

- An optimization algorithm based on 'ant colony behavior' has been developed
- •It allows the efficient implementation of variance reduction techniques
- •It uses the information scored on importance maps
- Minimum intervention by the user is required ... but details are relevant





